

The Addition Principle (The Rule of Sum)

- If A and B are disjoint events with n_1 and n_2 possible outcomes, respectively, then the total number of possible outcomes for event (A **or** B) is $n_1 + n_2$.
- If a first task can be performed in m ways, while a second task can be performed in n ways, and the two tasks cannot be performed simultaneously, then performing either task can be accomplished in any one of $m + n$ ways.
- If there are r_1 different objects in the first set, r_2 objects in the second set, ..., and r_m objects in the m^{th} set, and *if the different sets are disjoint*, then the number of ways to select an object from one of the m sets is $r_1 + r_2 + \dots + r_m$.
- Let S and T be finite sets. If S and T are disjoint, i.e., if $S \cap T = \emptyset$, then $|S \cup T| = |S| + |T|$.

[*Note:* this rule establishes a relationship between logical or, disjoint set union, and arithmetic addition.]

The Multiplication Principle (The Rule of Product)

- ❖ If there are n_1 possible outcomes for a first event and n_2 possible outcomes for a second event, there are $n_1 \cdot n_2$ possible outcomes for the sequence of the two events.
- ❖ If a procedure can be broken down into first and second stages, and if there are m possible outcomes for the first stage and if, for each of these outcomes, there are n possible outcomes for the second stage, then the total procedure can be carried out, in the designated order, in mn ways.
- ❖ Suppose a procedure can be *broken into m successive (ordered) stages*, with r_1 outcomes in the first stage, r_2 outcomes in the second stage, ..., and r_m outcomes in the m th stage. If the number of outcomes at each stage is independent of the choices in previous stages and if the composite outcomes are all distinct, then the total procedure has $r_1 \times r_2 \times \dots \times r_m$ different composite outcomes.
- ❖ For finite sets S_1, S_2, \dots, S_k , selecting one element from each set is equivalent to forming an element from the cartesian product of all the sets (a k -tuple).

$$|S_1 \times S_2 \times \dots \times S_k| = \prod_{j=1}^k |S_j|$$

[*Note:* this rule establishes a relationship between logical and, set cartesian product, and arithmetic multiplication.]