

1) For each of the following languages over the alphabet  $\Sigma = \{0, 1\}$  construct

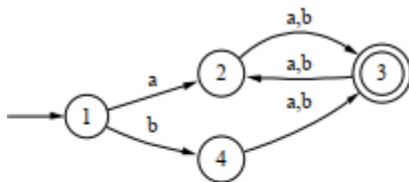
- a) a regular expression
  - b) a finite state automaton
  - c) a regular grammar
- i.  $\{w : w \text{ consists of any number of 0s and an even number of 1s}\}$
  - ii.  $\{w : \text{the length of } w \text{ is } 4i+1 \text{ for some } i \geq 0\}$
  - iii.  $\{w : \text{the length of } w \text{ is } 4i+1 \text{ for some } i \geq 0 \text{ and } w \text{ ends with a 0}\}$
  - iv.  $\{w : w \text{ does not contain either } 00 \text{ or } 11 \text{ as substrings}\}$
  - v.  $\{w : w \text{ contains } 00100 \text{ as a substring}\}$
  - vi.  $\{001, 1, 1010\}$

2) Describe in concise English the property or properties shared by all of the strings in the languages described by the following regular expressions. For example  $(0+1)(0+1)$  is the language of **all strings of length 2** over the alphabet  $\Sigma = \{0, 1\}$ .

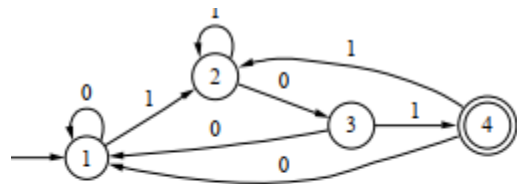
- i.  $(0+1)^*01$
- ii.  $1^*01^*$
- iii.  $(11)^*$
- iv.  $(0+1)^*1100(0+1)^*$
- v.  $1^*0^*$
- vi.  $0(0+1)^*0 + 1(0+1)^*1$

3) Describe the languages accepted by the following automata. You may use English or regular expressions to express your answer.

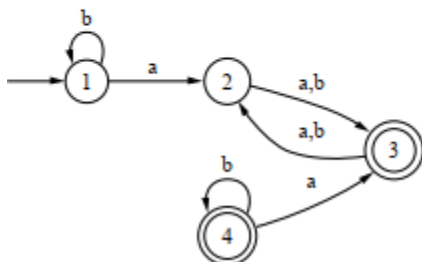
i.



iii,



ii.



iv.

