

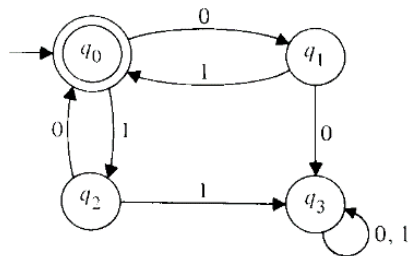
- 1) Prove that the number of strings over an alphabet is countably infinite. In other words, provide a 1-1 correspondence between the set of all possible strings and the natural numbers.
- 2) Draw an FSA state diagram for the following formal definition:

$$\Sigma = \{p, q, r\} \quad K = \{1, 2, 3, 4\} \quad F = \{2, 4\} \quad s = 1$$

$$\delta =$$

	<i>p</i>	<i>q</i>	<i>r</i>
1	1	3	2
2	4	4	2
3	2	3	4
4	1	2	3

- 3) For the following Finite State Machine state diagram write the formal definition (identify  $\Sigma$ ,  $K$ ,  $F$ ,  $s$ , &  $\delta$ )



- 4) Construct a finite state machine for each of the following languages  $\Sigma = \{a, b\}$ .
  - a)  $\{w : w \text{ has an even length}\}$
  - b)  $\{w : w \text{ contains the substring } abbb\}$
  - c)  $\{w : w \text{ begins and ends with the same symbol}\}$
  - d)  $\{w : |w| < 3\}$
  - e)  $\{w : w \text{ contains no } b\text{'s}\}$
  - f)  $\{baba\}$