

Homework Day #31
COMP 2230
Spring 2024
Prof. Stucki

1) Determine whether each of the following is true or false.

- a) $\emptyset \subseteq \emptyset$
- b) $\emptyset \in \emptyset$
- c) $\emptyset \in \{\emptyset\}$
- d) $\emptyset \subseteq \{\emptyset\}$
- e) $\varepsilon \subseteq \{\varepsilon\}$
- f) $\varepsilon \in \{\varepsilon\}$
- g) $\{\varepsilon\} = \emptyset$
- h) $\{a, b\} \in \{a, b, \{a, b\}\}$
- i) $\{a, b\} \subseteq \{a, b, \{a, b\}\}$
- j) $\{a, b\} \subseteq 2^{\{a, b, \{a, b\}\}}$
- k) $\{\{a, b\}\} \in 2^{\{a, b, \{a, b\}\}}$

2) Give three positive and three negative examples (if possible) of strings in the following languages, where $\Sigma = \{a, b\}$. In other words, list 3 strings that are in the language (positive) and three strings that are not in the language (negative).

- a) $\{w : w \text{ has an even length}\}$
- b) $\{w : w \text{ contains either the substring } abbb \text{ or the substring } aa\}$
- c) $\{w : w \text{ has twice as many } a\text{'s as } b\text{'s}\}$
- d) $\{w : w \text{ contains only } b\text{'s}\}$
- e) $\{w : w \text{ is a palindrome}\}$
- f) $\{w : w \text{ does not contain the substring } ba\}$

3) For each of the languages in question 2, determine whether the empty string, ε , is in the language.